## Maths for Computing Tutorial 14

1. Prove that  $L = \{ \alpha \mid M_{\alpha} \text{ is a Turing machine that accepts at least one input} \}$  is undecidable but recognisable.

- 2. Prove that  $E_{TM} = \{ \alpha \mid L(M_{\alpha}) = \emptyset \}$  is undecidable.
- 3. Prove that  $EQ_{TM} = \{(\alpha_1, \alpha_2) \mid L(M_{\alpha_1}) = L(M_{\alpha_2})\}$  is undecidable.